

# Algebra Review for GEOMETRY HONORS

Leave all answers as an EXACT answer. Do not round! This means you will have rational answers ( $\frac{a}{b}$ ), radical answers ( $\sqrt{a}$ ), and answers in terms of  $\pi$  ( $a\pi$ ). In Geometry Honors you will be required to leave your answers as EXACT values unless you use right triangle trigonometry (SOH-CAH-TOA). That means 90+% of your answers will be exact answers. It is important to practice number sense for this reason.

## Objective 1: Solving equations.

1) Solve each equation.

a)  $-158 = 7 + 3(1 - 7x)$

$$\begin{aligned} -155 &= 3(1 - 7x) \\ -155 &= 1 - 7x \end{aligned}$$

$$-56 = -7x$$

$$\boxed{8 = x}$$

c)  $-8(-2r - 3) = -36 + 6r$

$$\begin{aligned} 16r + 24 &= -36 + 6r \\ 10r + 24 &= -36 \end{aligned}$$

$$10r = -60$$

$$\boxed{r = -6}$$

e)  $\frac{4}{n-5} = \frac{10}{n+11}$

$$\begin{aligned} 10(n-5) &= 4(n+11) \\ 10n - 50 &= 4n + 44 \end{aligned}$$

$$14n = 94$$

$$\boxed{n = \frac{47}{7}}$$

g)  $\frac{2}{3}x + \frac{1}{2}x = \frac{3}{4}$

$$\frac{4}{6}x + \frac{3}{6}x = \frac{3}{4}$$

$$\boxed{x = \frac{18}{28} = \frac{9}{14}}$$

2) Solve the literal equations for the variable specified.

a)  $d = rt$ ; solve for t

$$\frac{d}{r}, r \neq 0$$

c)  $V = \frac{1}{3}\pi r^2 h$ ; solve for h

$$\boxed{h = \frac{3V}{\pi r^2}, r \neq 0}$$

3.  $\frac{V}{\pi r^2} = \frac{1}{3}h \cdot 3$

b)  $164 = 4 - 20n$

$$160 = -20n$$

$$\boxed{-8 = n}$$

d)  $5 + 4(6m - 3) = -39 + 8m$

$$5 + 24m - 12 = -39 + 8m$$

$$-7 + 24m = -39 + 8m$$

$$-7 + 16m = -39$$

$$16m = -32$$

$$\boxed{m = -2}$$

f)  ~~$x+6 = 10$~~

$$2(x+4) = 10(x-2)$$

$$x+4 = 5(x-2)$$

$$x+4 = 5x - 10$$

$$4 = 4x - 10$$

$$4 = 4x$$

$$\boxed{\frac{1}{4} = 1 = x}$$

h)  $\frac{x}{2} + 1 = \frac{5}{4}$

$$\frac{x}{2} + \frac{4}{4} = \frac{5}{4}$$

$$2 \cdot \frac{x}{2} = \frac{1}{4} \cdot 2$$

$$\boxed{x = \frac{2}{4} = \frac{1}{2}}$$

b)  $P = 2w + 2l$ ; solve for w

$$-2l = -2l$$

$$\frac{P-2l}{2} = \frac{2w}{2}$$

$$\boxed{w = \frac{P-2l}{2} \text{ OR } w = \frac{P}{2} - l}$$

d)  $y = \frac{c-ax}{b}$ ; solve for x

$$\frac{yb}{c} = c - ax$$

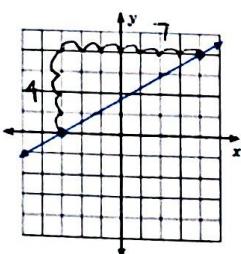
$$yb - c = -ax$$

$$\boxed{\frac{yb-c}{-a} = x, a \neq 0}$$

## Objective 2: Linear equations.

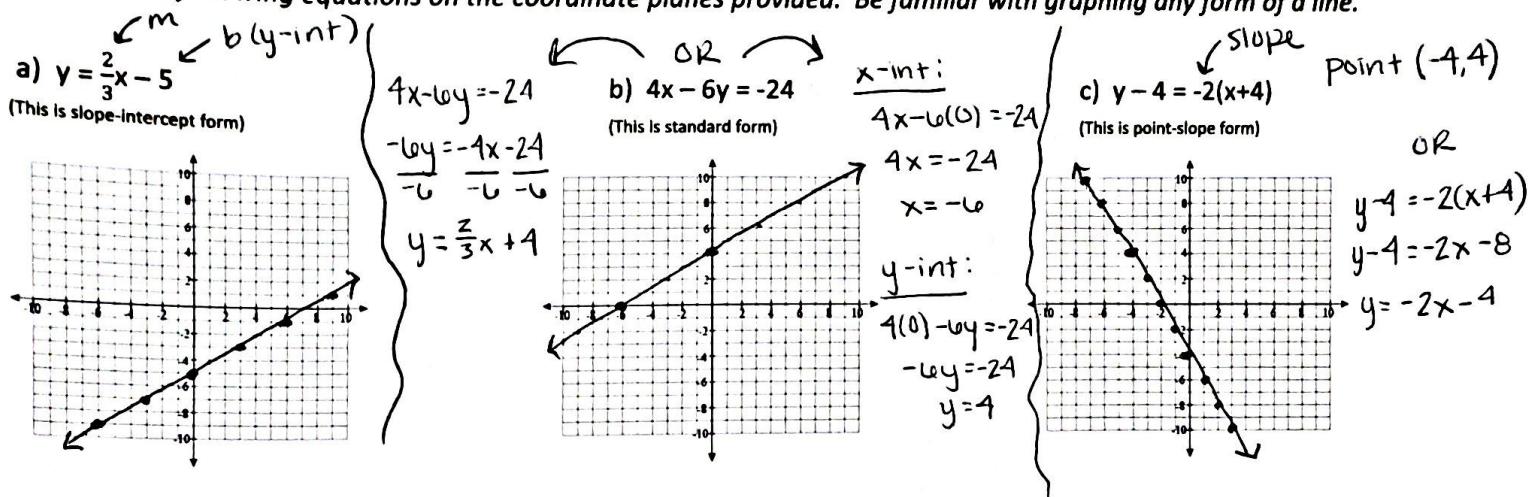
3) Find the slope of the line.

$\downarrow$   
rise  
run



$$\boxed{m = \frac{4}{3}}$$

4) Graph the following equations on the coordinate planes provided. Be familiar with graphing any form of a line.



5) Write the equation of the line in slope-intercept form using the given information.

a) slope =  $\frac{3}{4}$ ; y-intercept is  $(0, -5)$

$$y = \frac{3}{4}x - 5$$

b) slope = -3 and passes through  $(4, -3)$

$$y + 3 = -3(x - 4)$$

OR  $y = mx + b$   
 $-3 = -3(4) + b$   
 $-3 = -12 + b$   
 $9 = b$

c) slope =  $\frac{2}{3}$  and passes through  $(-3, 5)$

$$y - 5 = \frac{2}{3}(x + 3)$$

$$\begin{aligned} y &= mx + b \\ 5 &= \frac{2}{3}(-3) + b \\ 5 &= -2 + b \\ 7 &= b \end{aligned}$$

$$y = \frac{2}{3}x + 7$$

d) passes through  $(-2, 4)$  and  $(0, -1)$

$$m = \frac{4 - 1}{-2 - 0} = \frac{3}{-2}$$

$$y = -\frac{3}{2}x - 1$$

### Objective 3: Systems of Linear Equations

6) Solve each system of equations by the substitution method.

a)  $y = 2x + 5$

$$3x - y = 4$$

$$3x - (2x + 5) = 4$$

$$3x - 2x - 5 = 4$$

$$x - 5 = 4$$

$$x = 9$$

$$(9, 23)$$

b)  $8x + 3y = 26$

$$2x = y - 4 \rightarrow y = 2x + 4$$

$$8x + 3(2x + 4) = 26$$

$$8x + 6x + 12 = 26$$

$$14x + 12 = 26$$

$$14x = 14$$

$$x = 1$$

$$y = 2(1) + 4$$

$$y = 2 + 4$$

$$y = 6$$

$$(1, 6)$$

7) Solve each system of equations by the elimination method.

a)  $\begin{cases} 3x + 4y = 9 \\ -3x - 2y = -3 \end{cases}$

$$3x + 4(3) = 9$$

$$3x + 12 = 9$$

$$2y = 6$$

$$y = 3$$

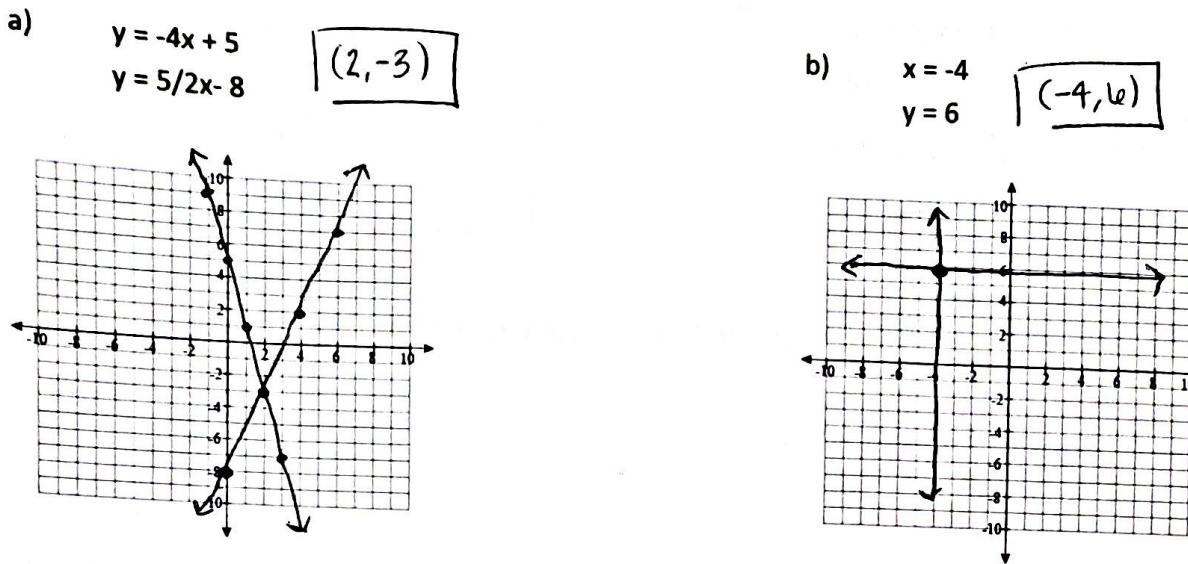
$$(-1, 3)$$

b)  $\begin{cases} 4x - 6y = -24 \\ -2x + 3y = 13 \end{cases}$

$$\begin{array}{r} 4x - 6y = -24 \\ -2x + 3y = 13 \\ \hline 0 = 0 \end{array}$$

Identity; infinitely many solutions

8) Solve each system of equations by the graphing method.



#### Objective 4: Quadratic equations and expressions.

9) Factor the expression completely.

a)  $v^2 - 19v + 90$

$\boxed{(v-10)(v-9)}$

b)  $5a^2 + 38a - 63 =$

$\begin{array}{r} -315 \\ \cancel{45} \quad \cancel{-7} \\ \cancel{38} \end{array}$

$$\begin{aligned} 5a^2 + 45a - 7a - 63 \\ 5a(a+9) - 7(a+9) \end{aligned}$$

c)  $5p^2 - 4p$

$\boxed{p(5p-4)}$

$$\begin{array}{r} -270 \\ \cancel{27} \quad \cancel{-10} \\ \cancel{17} \end{array}$$

d)  $36x^2 + 68xy - 120y^2 =$

$\begin{array}{r} -216 \\ \cancel{9} \quad \cancel{17} \\ \cancel{8} \end{array}$

$$\begin{aligned} 9x^2 + 21xy + 10xy - 30y^2 \\ 9x(x+3y) - 10y(x+3y) \end{aligned}$$

10) Solve the quadratic equation or proportion by factoring and using the zero product property. Hint: Use the AC method. MUST EQUAL ZERO FIRST!

a)  $x^2 + 6x + 8 = 0$

$$(x+2)(x+4) = 0$$

$$\begin{array}{l} x+2=0 \\ \boxed{x=-2} \end{array} \quad \begin{array}{l} x+4=0 \\ \boxed{x=-4} \end{array}$$

b)  $x^2 + 5x + 6 = -x^2 - 3x \rightarrow 2x^2 + 8x + 6 = 0$

$$2(x^2 + 4x + 3) = 0$$

$$x+3=0 \quad x+1=0$$

$$\boxed{x=-3} \quad \boxed{x=-1}$$

c)  $3x^2 + 7x - 8 = -10$

$$3x^2 + 7x + 2 = 0$$

$$3x^2 + 6x + x + 2$$

$$3x(x+2) + 1(x+2)$$

$$\overbrace{\frac{x+2}{5}}^{x+2} = \frac{4}{x+1}$$

$$(x+2)(x+1) = 20$$

$$x^2 + x + 2x + 2 = 20$$

$$x^2 + 3x + 2 = 20$$

$$x^2 + 3x - 18 = 0$$

$$\begin{array}{r} 6 \\ \cancel{6} \quad \cancel{1} \\ \cancel{7} \end{array}$$

$$(3x+1)(x+2) = 0$$

$$\begin{array}{l} 3x+1=0 \\ \boxed{x=-\frac{1}{3}} \end{array} \quad \begin{array}{l} x+2=0 \\ \boxed{x=-2} \end{array}$$

d)  $2x^2 - 4x + 2 = 0$

$$2(x^2 - 2x + 1) = 0$$

$$2(x-1)^2 = 0$$

$$x-1=0$$

$$\boxed{x=1}$$

f)  $\frac{2}{x-3} = \frac{x-2}{6}$

$$(x-3)(x-2) = 12$$

$$x^2 - 2x - 3x + 6 = 12$$

$$x^2 - 5x + 6 = 12$$

$$x^2 - 5x - 6 = 0$$

$$(x-6)(x+1) = 0$$

$$\boxed{x=6} \quad \boxed{x=-1}$$

11) Solve for  $x$  using the quadratic formula. Hint:  $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

$$a=1 \quad b=-3 \quad c=1$$

a)  $x^2 - 3x + 1 = 0$

$$x = \frac{3 \pm \sqrt{(-3)^2 - 4(1)(1)}}{2(1)}$$

$$x = \frac{3 \pm \sqrt{5}}{2}$$

$$x = \frac{3 \pm \sqrt{5}}{2}$$

$$a=5 \quad b=2 \quad c=-2$$

b)  $5x^2 + 2x - 2 = 0$

$$x = \frac{-2 \pm \sqrt{(2)^2 - 4(5)(-2)}}{2(5)}$$

$$x = \frac{-2 \pm \sqrt{44}}{10} = \frac{-2 \pm 2\sqrt{11}}{10} = \boxed{\frac{-1 \pm \sqrt{11}}{5}}$$

12) Solve the equation and express your answer as an EXACT value.

a)  $3^2 + 4^2 = x^2$

$$9 + 16 = x^2$$

$$\sqrt{25} = x^2$$

$$\boxed{\pm 5 = x}$$

c)  $1^2 + x^2 = 3^2$

$$1 + x^2 = 9$$

$$\sqrt{x^2} = \sqrt{8}$$

$$\boxed{x = \pm 2\sqrt{2}}$$

b)  $x^2 + 5^2 = 13^2$

$$x^2 + 25 = 169$$

$$\sqrt{x^2} = \sqrt{144}$$

$$\boxed{x = \pm 12}$$

d)  $x^2 + (7\sqrt{3})^2 = (2x)^2$

$$x^2 + 147 = 4x^2$$

$$147 = 3x^2$$

$$\sqrt{49} = \sqrt{x^2}$$

$$\boxed{x = \pm 7}$$

## Objective 5: Radical Expressions

13) Simplify the radical expression completely. Leave your answer in simplest radical form.

a)  $\sqrt{50} = \sqrt{25} \cdot \sqrt{2}$   
 $= \boxed{5\sqrt{2}}$

b)  $\sqrt{600} = \sqrt{100} \cdot \sqrt{6}$   
 $= \boxed{10\sqrt{6}}$

c)  $-2\sqrt{216pq^3r^5} = \boxed{-12qr^2\sqrt{6pqr}}$   
 $= -2\sqrt{36} \cdot \sqrt{6} \cdot \sqrt{p} \cdot \sqrt{q^2} \cdot \sqrt{q} \cdot \sqrt{r} \cdot \sqrt{r}$   
 $= -2 \cdot 6 \cdot \sqrt{6} \cdot \sqrt{p} \cdot q \cdot \sqrt{q} \cdot r^2 \cdot \sqrt{r}$

d)  $-3\sqrt{70x} = \boxed{-3\sqrt{70x}}$

e)  $\sqrt{6} \cdot \sqrt{2} = \sqrt{12} = \sqrt{4} \cdot \sqrt{3}$   
 $= \boxed{2\sqrt{3}}$

f)  $\sqrt{3} \cdot \sqrt{3} = \sqrt{9}$   
 $= \boxed{3}$

g)  $\frac{\sqrt{4}}{\sqrt{64}} = \frac{2 \cdot 2}{8} = \frac{4}{8} = \boxed{\frac{1}{2}}$

h)  $\frac{2\sqrt{6}}{5\sqrt{27}} = \frac{2\sqrt{2} \cdot \sqrt{3}}{5 \cdot \sqrt{9} \cdot \sqrt{3}} = \frac{2\sqrt{2}}{5 \cdot 3} = \boxed{\frac{2\sqrt{2}}{15}}$

i)  $5\sqrt{5} + 4\sqrt{5} = \boxed{9\sqrt{5}}$

j)  $-\sqrt{18} + 2\sqrt{2}$   
 $\downarrow$   
 $-\sqrt{9} \cdot \sqrt{2} + 2\sqrt{2}$   
 $-3\sqrt{2} + 2\sqrt{2} = \boxed{-1\sqrt{2}}$

k)  $\sqrt{13^2} = \boxed{13}$

l)  $(2\sqrt{3})^2 = (2\sqrt{3})(2\sqrt{3})$   
 $= 4\sqrt{9}$   
 $= 4 \cdot 3 = \boxed{12}$

## Objective 6: Simplify algebraic expressions.

14) Simplify each algebraic expression.

a)  $(2x)^2 = (2x)(2x)$   
 $= \boxed{4x^2}$

b)  $(-2x)^2 = (-2x)(-2x)$   
 $= \boxed{4x^2}$

c)  $-(2x)^2 = -(2x)(2x)$   
 $= \boxed{-4x^2}$

d)  $y(3y^2 - 5y - 10)$   
 $\boxed{3y^3 - 5y^2 - 10y}$

e)  $(x+4)^2 = (x+4)(x+4)$   
 $= x^2 + 4x + 4x + 16$   
 $= \boxed{x^2 + 8x + 16}$

f)  $\overbrace{(2x^2 - 3x)(-4x^2 + 5)}^{= -8x^4 + 10x^2 + 12x^3 - 15x}$   
 $= -8x^4 + 12x^3 + 10x^2 - 15x$

g)  $(x+3)(x-7)$   
 $x^2 - 7x + 3x - 21$   
 $\boxed{x^2 - 4x - 21}$

h)  $\frac{8w}{2} = \frac{2 \cdot 4w}{2} = \boxed{4w}$

i)  $\frac{5x-10}{15} = \frac{5(x-2)}{5 \cdot 3} = \boxed{\frac{x-2}{3}}$

j)  $\frac{x+6}{x^2-36} = \frac{(x+6)}{(x+6)(x-6)}$   
 $= \boxed{\frac{1}{x-6}}, x \neq 6$

k)  $\frac{33ab-22b}{11b} = \frac{11b(3a-2)}{11b}$   
 $= \boxed{3a-2}$

l)  $\frac{5a+5b}{a^2-b^2} = \frac{5(a+b)}{(a+b)(a-b)}$   
 $= \boxed{\frac{5}{a-b}}, a \neq b$